
Predicting Sedimentary Facies in the Gulf of Mexico Region from the Combination of Bathymetry, Gravity, and Magnetic Data Using Fractal Geometry

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ABSTRACT

Lamb et al. (2004) identified from flume experiments four regimes of deposition, mathematically described by a Ponding Index (Po): (1) a perfectly ponded deposit, (2) a mounded deposit, (3) a perfectly draped deposit, and (4) a deposit with accentuated highs. This study extends Lamb's laboratory results to basin scale architecture by using bathymetry, gravity, and magnetics combined with fractal geometry to predict the same four sedimentary facies in the Gulf of Mexico region.

Turcotte (1992) first published *Fractals and Chaos in Geology and Geophysics* 25 years ago. Data that exhibit power-law spectra, such as bathymetry, gravity, and magnetics, are suitable for the application of fractal geometry. The fractal dimension of the combination of bathymetry and gravity (FDBG) identifies a preferred depositional pattern working from the top down through geologic time. Likewise, combining magnetics and gravity with fractal geometry (FDMG) identifies a preferred depositional pattern working from the bottom up through geologic time. Taking the ratio FDBG/FDMG yields a Ratio Index (Ro) map similar to Lamb's Po.

After 70 years of drilling in the Gulf of Mexico, many fields correlate well with Ro. The expanded Miocene discoveries (e.g., Thunderhorse) in the deepwater Gulf of Mexico are examples of ponded deposits. There are also several large mounded deposit fields (e.g., Mars). This study presents an Ro map over the Gulf of Mexico showing the four sedimentary facies identified in the Lamb et al. (2004) paper. Examples of all four depositional regimes are shown on several 2D seismic lines (GulfSPAN). The study area extends down to the Yucatan Peninsula where Ro shows a diagnostic footprint of the Chicxulub Impact. The study thus discusses other possible impact sites in the Gulf of Mexico based on Ro.



Apache



09.19.2016

PREDICTING SEDIMENTARY FACIES

IN THE GOM REGION FROM THE COMBINATION OF BATHYMETRY,
GRAVITY, AND MAGNETICS USING FRACTAL GEOMETRY

VICTOR J. MISTRETТА

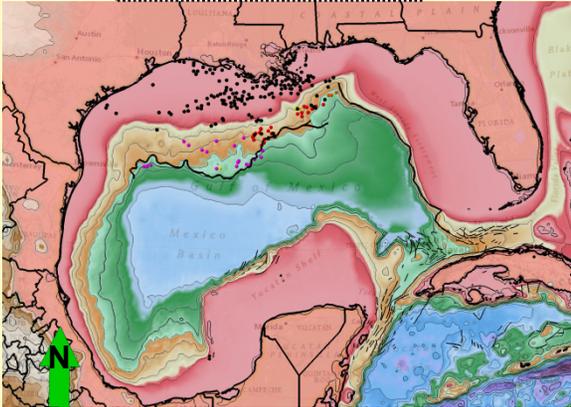


PREDICTING SEDIMENTARY FACIES

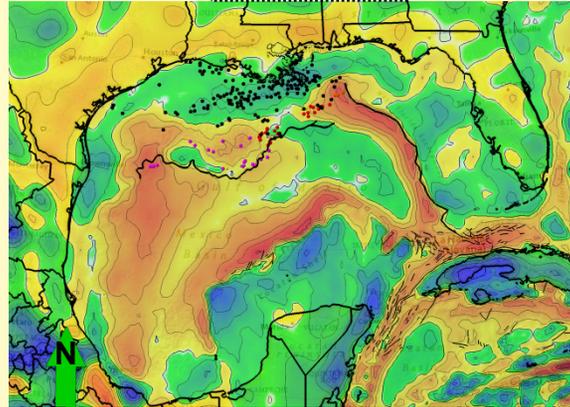
IN THE **GoM REGION** FROM THE **COMBINATION** OF



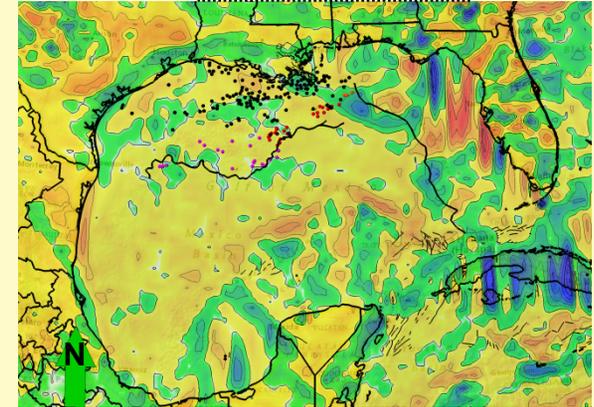
Bathymetry



Gravity



Magnetics



Gentle Fractal Landscape

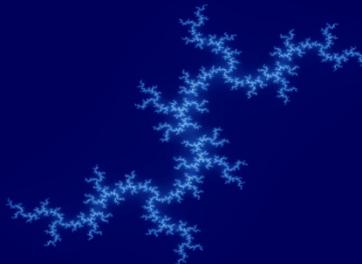


Using
FRACTAL GEOMETRY

Rugged Fractal Landscape



Dendritic Julia Set

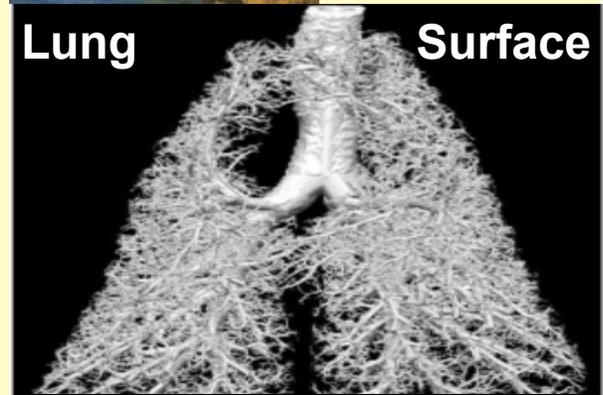


Fractal Dimension ~ 0.8

A Fractal is a nonlinear geometric object with an infinite nesting of facsimile structures at all scales (from outcrop to thin section).

Lung

Surface



Fractal Dimension ~ 2.97



DENDRITIC DRAINAGE PATTERNS

BUILDING A FRACTAL DRAINAGE NETWORK



$$N_n = C/(r_n)^D \Rightarrow D = \ln(N_{n+1}/N_n)/\ln(r_n/r_{n+1}) \quad \text{Donald Turcotte "Fractals and Chaos in Geology and Geophysics"}$$

Where N = # of Objects, C = Constant of Proportionality,
 r = Size or Linear Dimension, and D = Fractal Dimension.

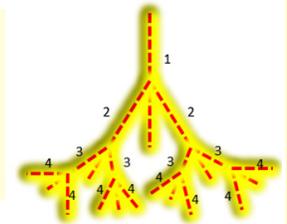


ASSUMPTIONS: (A) Linear Dimension of the Drainage Network is Represented by All Paleobathymetries (PB).
 (B) Ratio of Successive Paleobathymetries is constant insuring scale invariance.

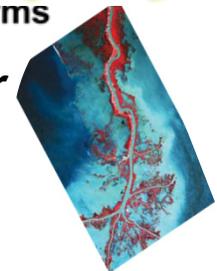
Thus from (A)
 And from (B)
 Substitution into (1)
 Factoring (3)
 Geometric Series [...]
 Hence
 And
 Substitution into (4)
 Likewise
 Hence
 Therefore

- (1) $r_n = PB_0 + PB_1 + PB_2 + PB_3 \dots$
- (2) $r = PB_0/PB_1 = PB_1/PB_2 = PB_2/PB_3 \dots$
- (3) $r_n = PB_0 + PB_0/r + PB_0/r^2 + PB_0/r^3 + \dots$
- (4) $r_n = PB_0r [1/r + 1/r^2 + 1/r^3 + \dots]$
- (5) with $a_1 = 1/r$, $a_n = 1/r^n$, $c = 1/r$ (common ratio), and n number of terms
- (6) $S_n = (1/r (1-1/r^n))/(1-1/r)$
- (7) $\lim_{n \rightarrow \infty} S_n = 1/r/(1-1/r) = 1/(r-1)$
- (8) $r_n = PB_0r/(r-1)$
- (9) $r_{n-1} = PB_1r/(r-1)$
- (10) $\ln(r_n/r_{n+1}) = \ln((PB_1r/(r-1)) \times ((r-1)/(PB_0r)) = \ln(PB_1/PB_0)$
- (11) $D = (\ln(2))/(\ln(PB_1/PB_0))$

After Time 1 ~ 1 Object
 After Time 2 ~ 2 Objects
 After Time 3 ~ 4 Objects
 After Time 4 ~ 8 Objects
 ...etc... Thus
 $N_{n+1}/N_n = 2$ where N = # of Objects



*Mississippi River
 Delta*



Iterating Paleobathymetries at Major Geologic Ages was complex and produced unfavorable results because of a paucity of input points. Gravity is tacitly a collage of all Paleobathymetries. This assumption reduced the above algorithm to a very simple formula.

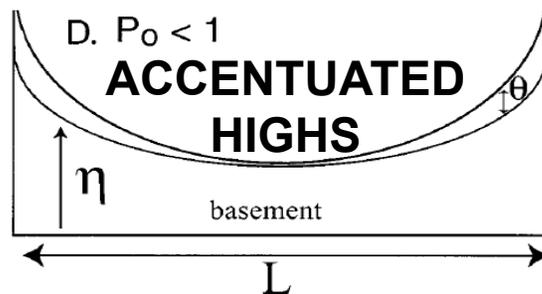
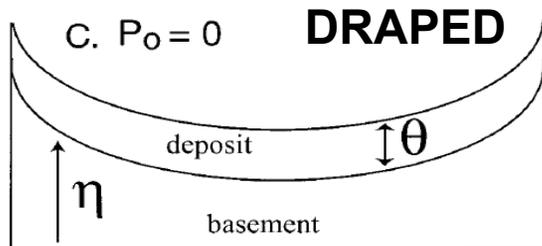
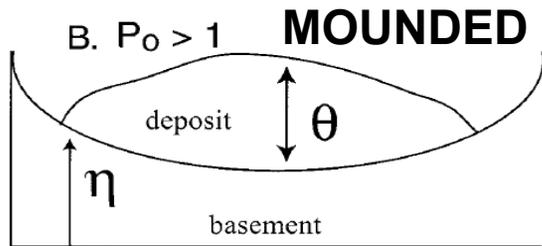
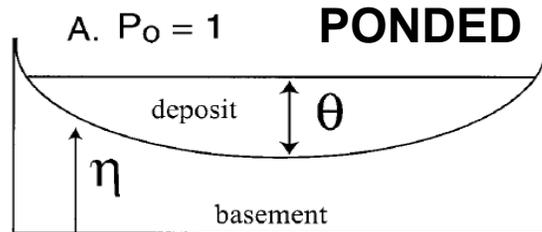
$$FDBG = (\ln(2))/(\ln(B+C/G+C'))$$

$$FDMG = (\ln(2))/(\ln(M/G))$$



DEPOSITIONAL REGIMES

LABORATORY STUDY OF TURBIDITY CURRENTS



Surging Flows

Continuous Flows

Michael P. Lamb, et al
Journal of
Sedimentary Research,
2004

$$P_o = -\frac{1}{L} \int_0^L \frac{d\theta}{d\eta} dx$$

Where x is the downdip coordinate, L denotes the streamwise length of the basin, $\theta(x)$ denotes the thickness of the deposit and $\eta(x)$ denotes the elevation of the initial bed. A deposit ponding index equal to one represents a completely ponded deposit (Fig. 4A), a deposit ponding index greater than unity represents a mounded deposit (Fig. 4B), and a deposit ponding index equal to zero represents a purely draped deposit (Fig. 4C). A deposit with accentuated highs, meaning that the flow deposits preferentially on the slopes rather than the center of the basin, would have a negative deposit ponding index (Fig. 4D).

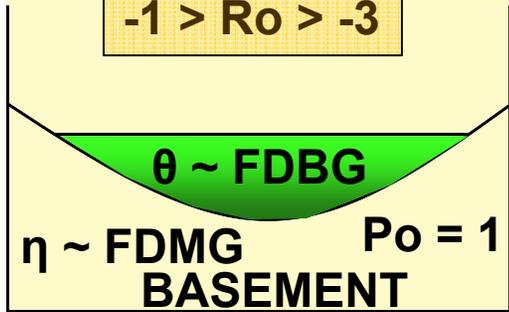
FIG. 4.—Four regimes of deposition described by the deposit ponding index are A) a perfectly ponded deposit: $P_o = 1$, B) a mounded deposit: $P_o > 1$, C) a perfectly draped deposit: $P_o = 0$, and D) a deposit with accentuated highs: $P_o < 0$.



RATIO INDEX MAP (Ro)

RELATION TO LAMB'S PONDING INDEX (Po)

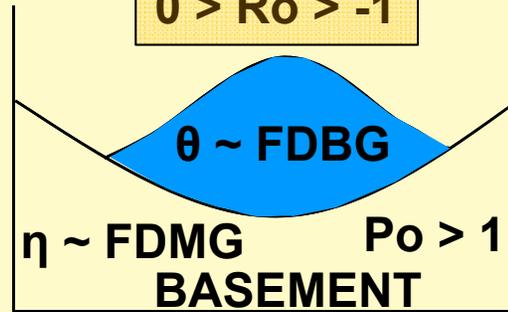
$$-1 > Ro > -3$$



PONDED

Expanded Miocene

$$0 > Ro > -1$$



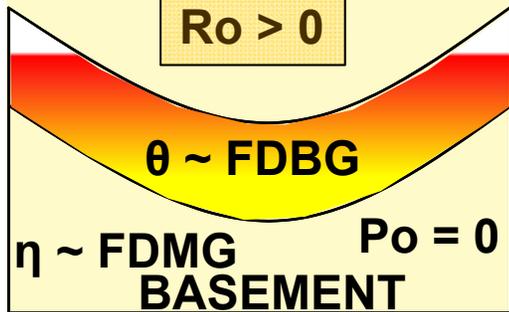
MOUNDED

'Auger' 'Lucius' 'Mars'

**Surging
Flows**

$|G| > |M|$
 $\Rightarrow \text{FDMG} (-)$
 If $|G| - |M| \approx 0$
 Then $Ro \approx 0(-)$

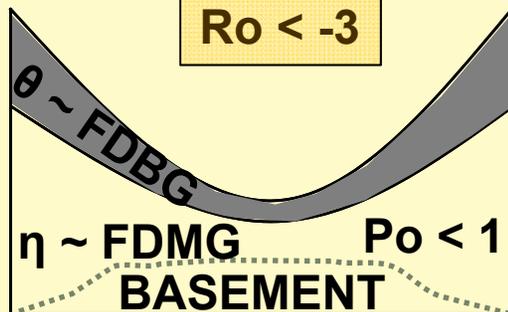
$$Ro > 0$$



DRAPED/PLANAR

Mississippi Fan

$$Ro < -3$$

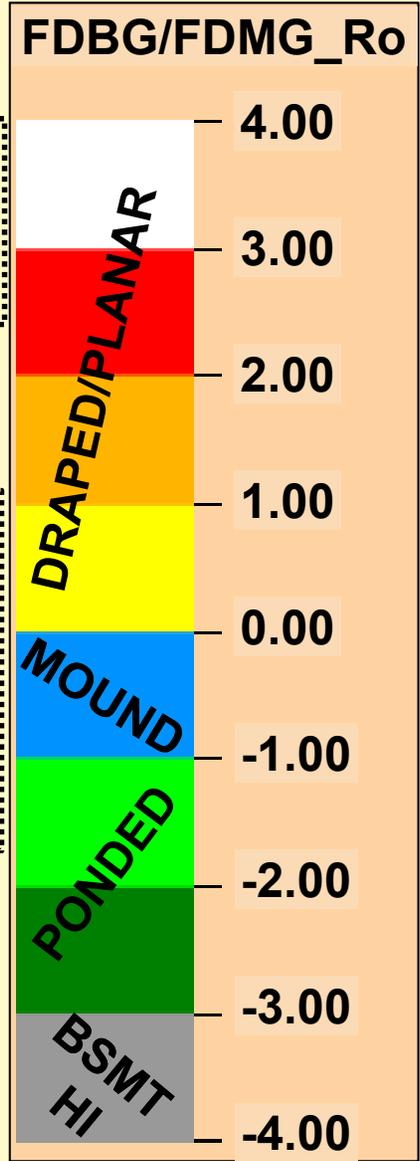


BASEMENT HIGH

Mexican Ridges

$|M| > |G|$
 $\Rightarrow \text{FDMG} (+)$
 $\Rightarrow Ro (+)$
 $|G| > |M|$
 $\Rightarrow \text{FDMG} (-)$
 If $|G| - |M| \uparrow$ ing
 Then $Ro < -3$

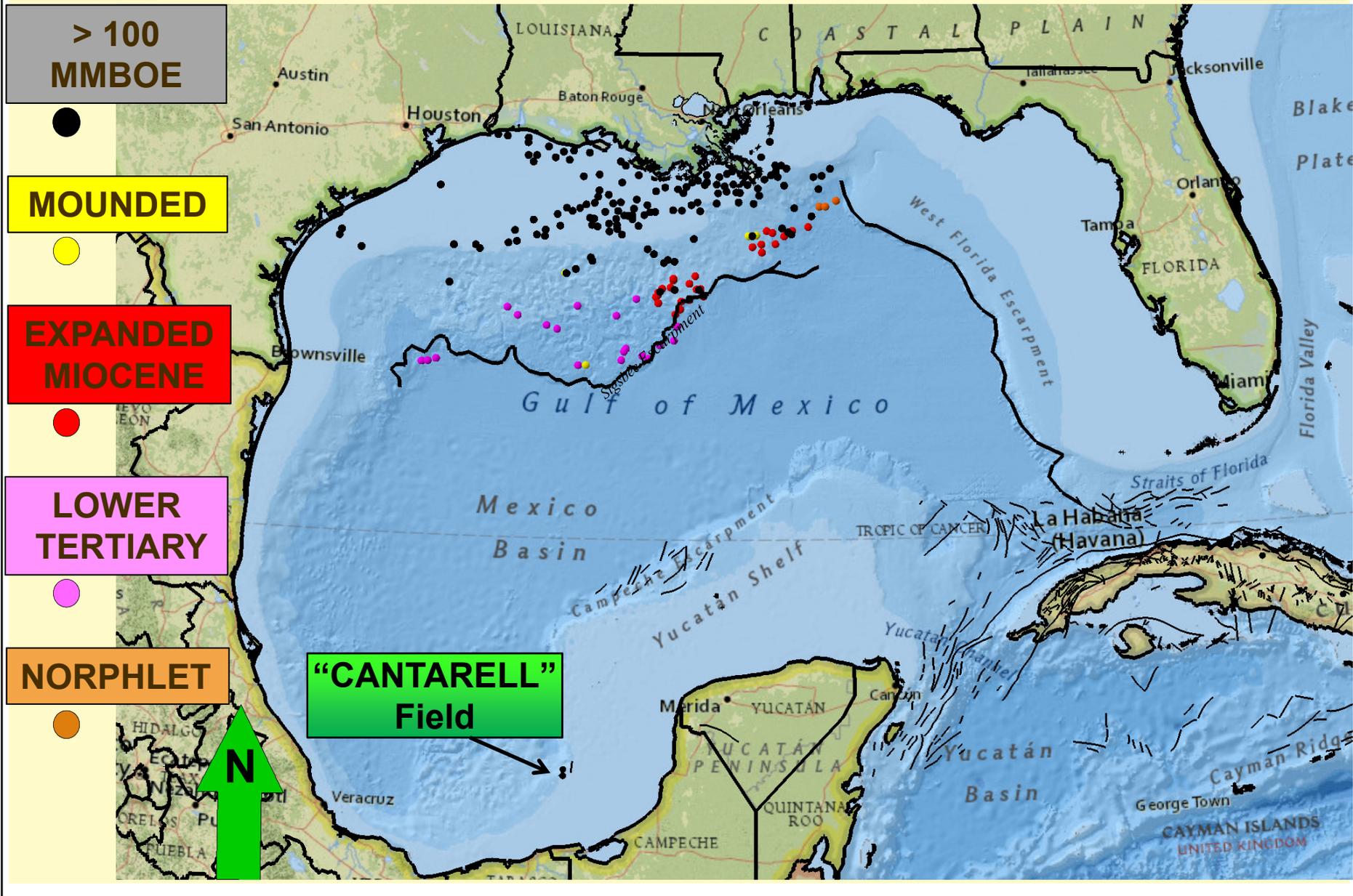
**Continuous
Flows**



FDBG = Fractional Dimension of Bathymetry & Gravity,
FDMG = Fractional Dimension of Magnetism & Gravity,
Ro = the ratio of FDBG over FDMG

GULF OF MEXICO STUDY AREA

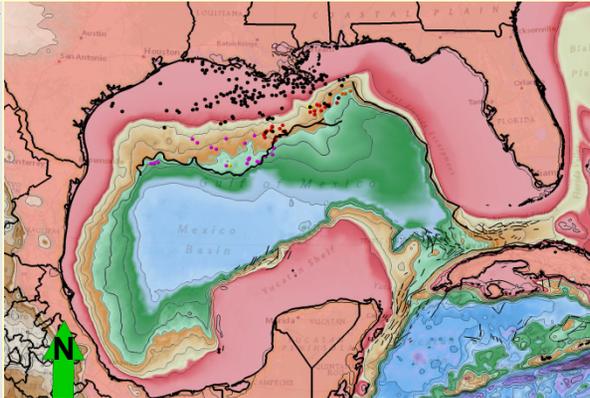
SIGNIFICANT FIELDS IN US WATERS



FRACTAL COMBINATION (FDBG) BATHYMETRY AND GRAVITY



BATHYMETRY

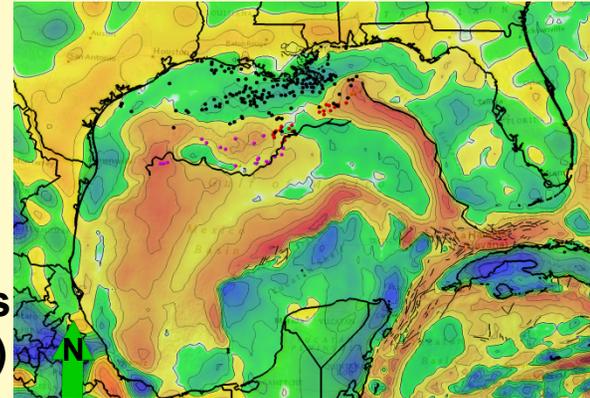
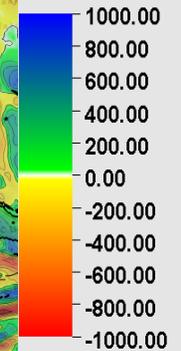


Wiggins Arch (WA)

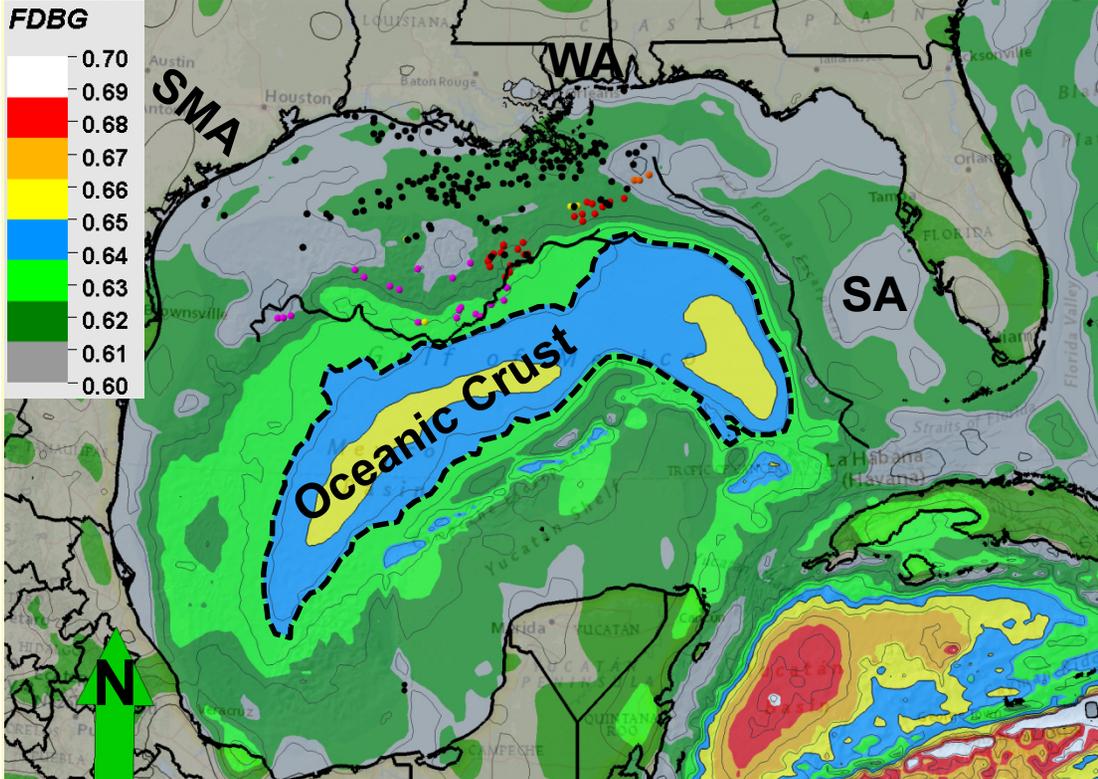
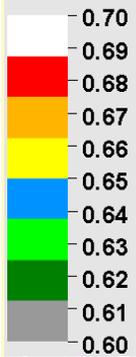
Sarasota Arch (SA)

San Marcos Arch (SMA)

GRAV ANOMALY

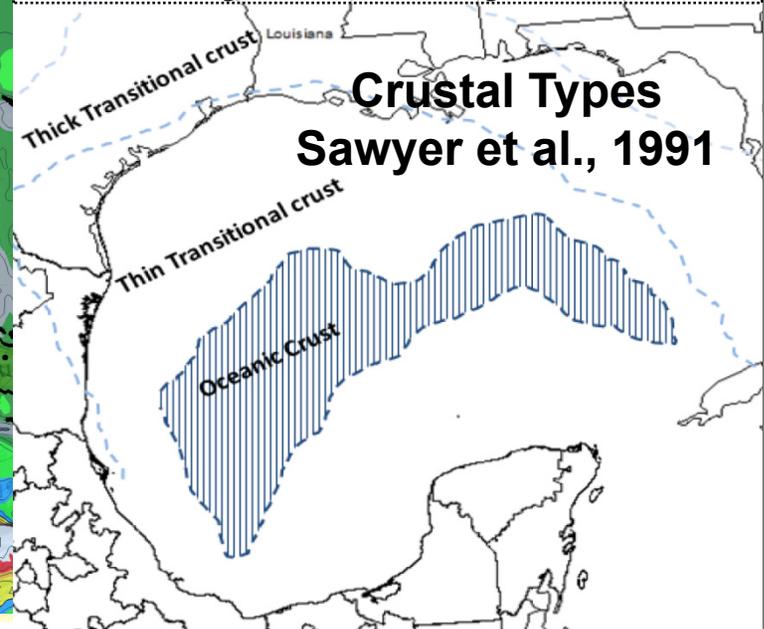


FDBG

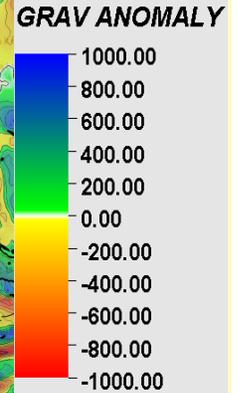
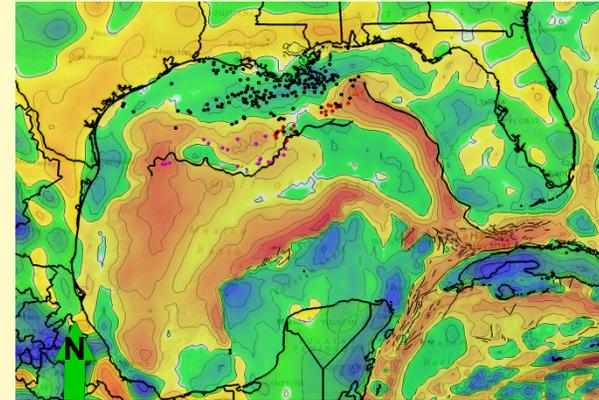
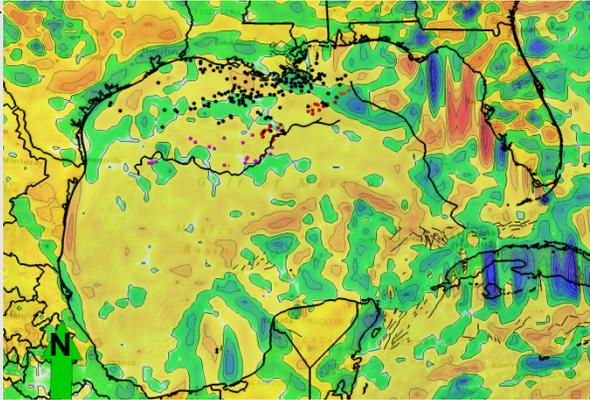
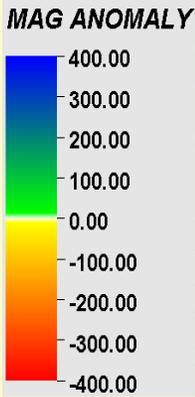


An Integrated Geophysical Study of the Northern GoM
Eray Kocel, May 2012

Crustal Types
Sawyer et al., 1991

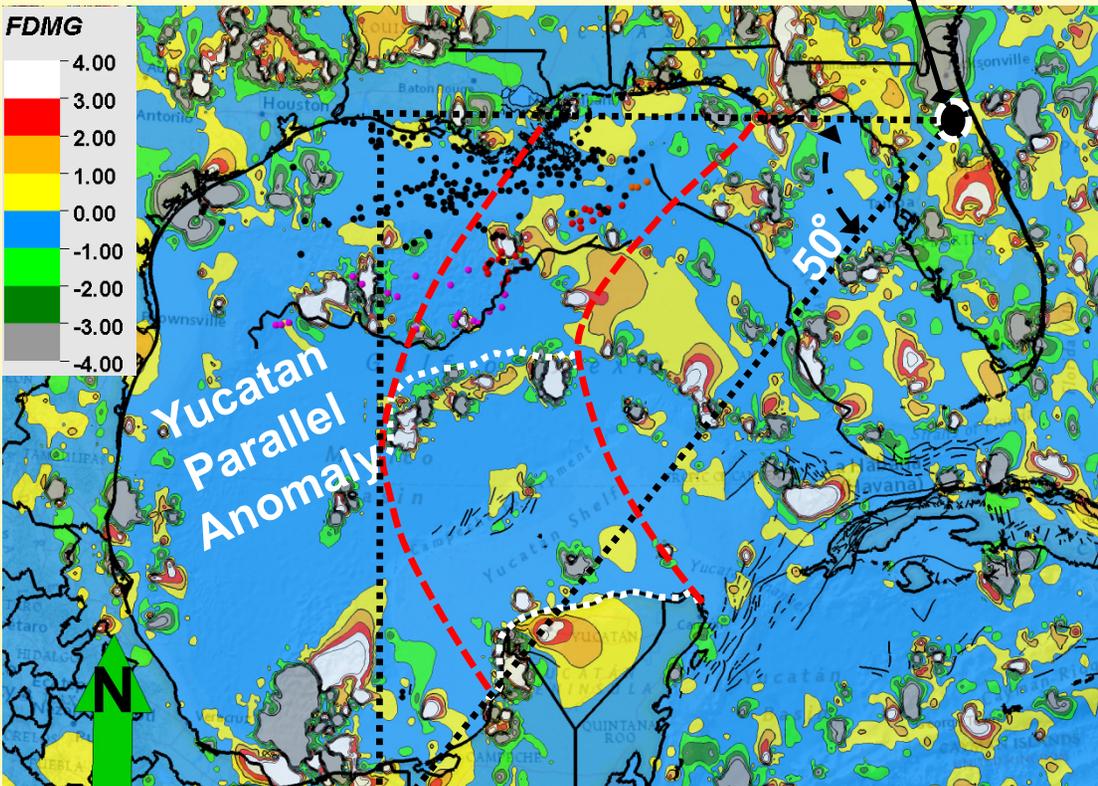


FRACTAL COMBINATION (FDMG) MAGNETICS AND GRAVITY

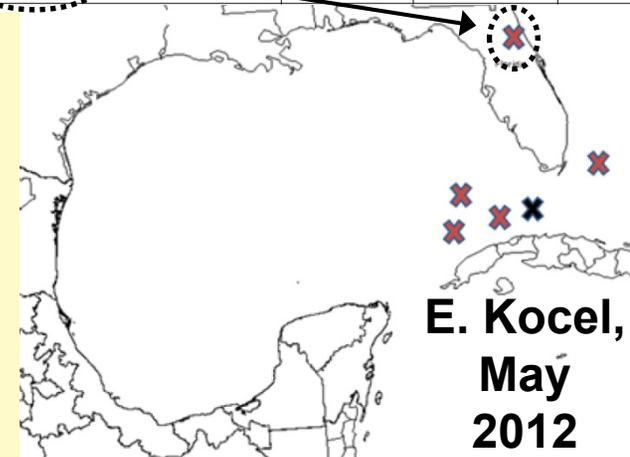


Pole of Rotation

FDMG



	Latitude	Longitude	Rotation
Dunbar and Sawyer, 1987	25.00	-79.00	45°
Hall and Najmuddin, 1994	24.00	-81.5	55°
Shepherd, 1983	24.00	-84.0	41°
Bird et al., 2005	24.00	-81.5	42°
Pindell, 1985	29.5	-81.4	43°





(FDMG) & (FDBG) COMPARED TO FRACTAL LANDSCAPES



Rugged Fractal
Landscape

Gentle Fractal
Landscape

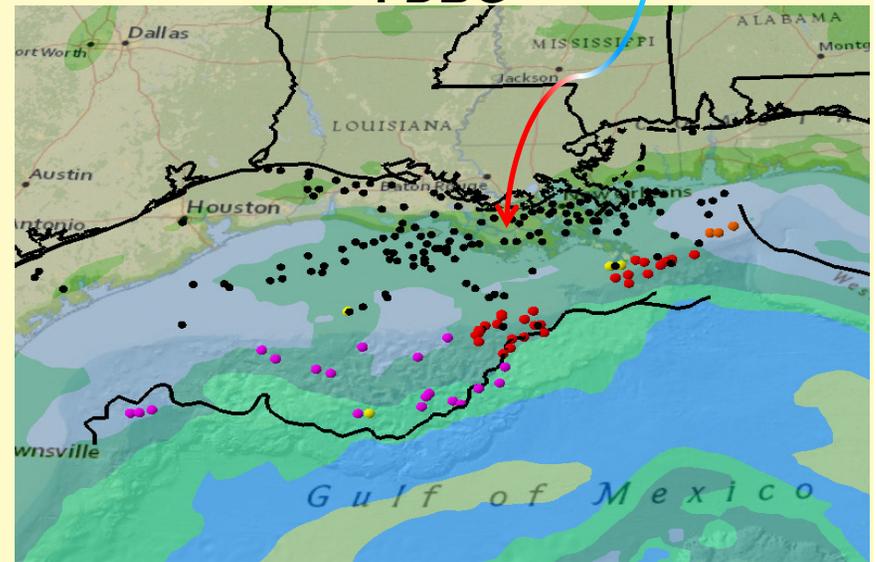
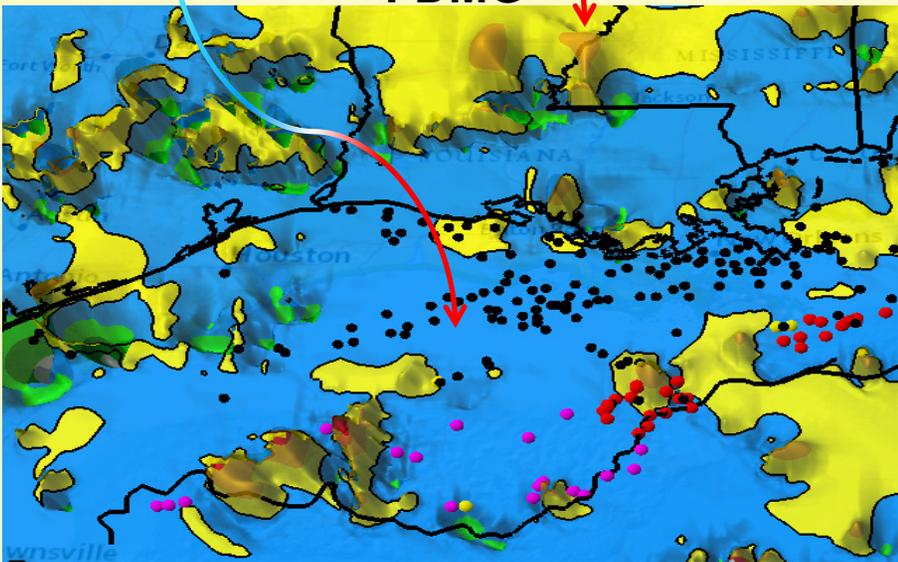
Magnetics Driven
(+) FDMG

Gravity Driven
(-) FDMG

(↑) FDBG
Bathymetry ~
Stack of Paleo
Bathymetries

FDMG

FDBG



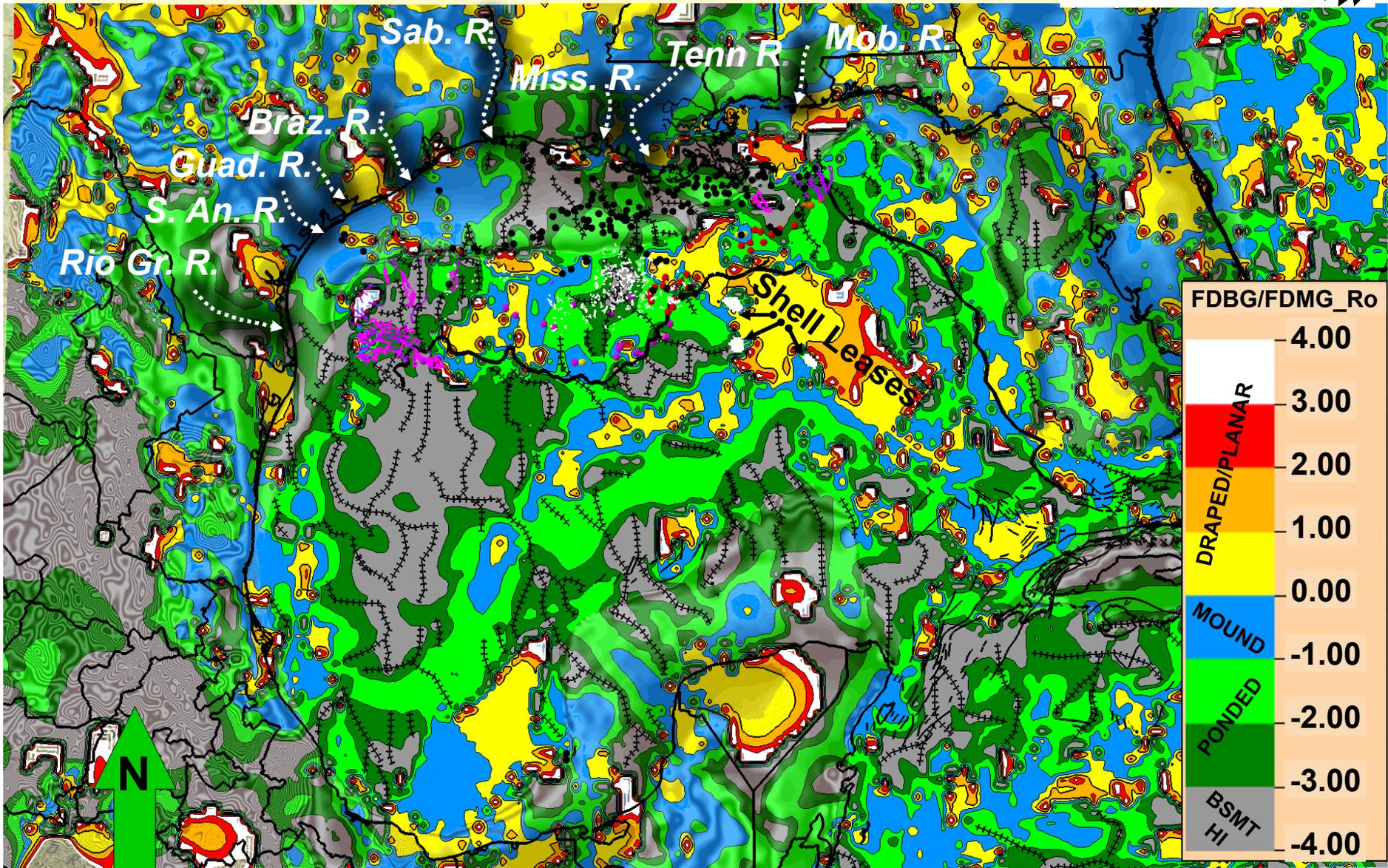


(R_o) RATIO OF FDBG OVER FDMG

ANCESTRAL RIVERS; BOEM SEEP ANOMALIES



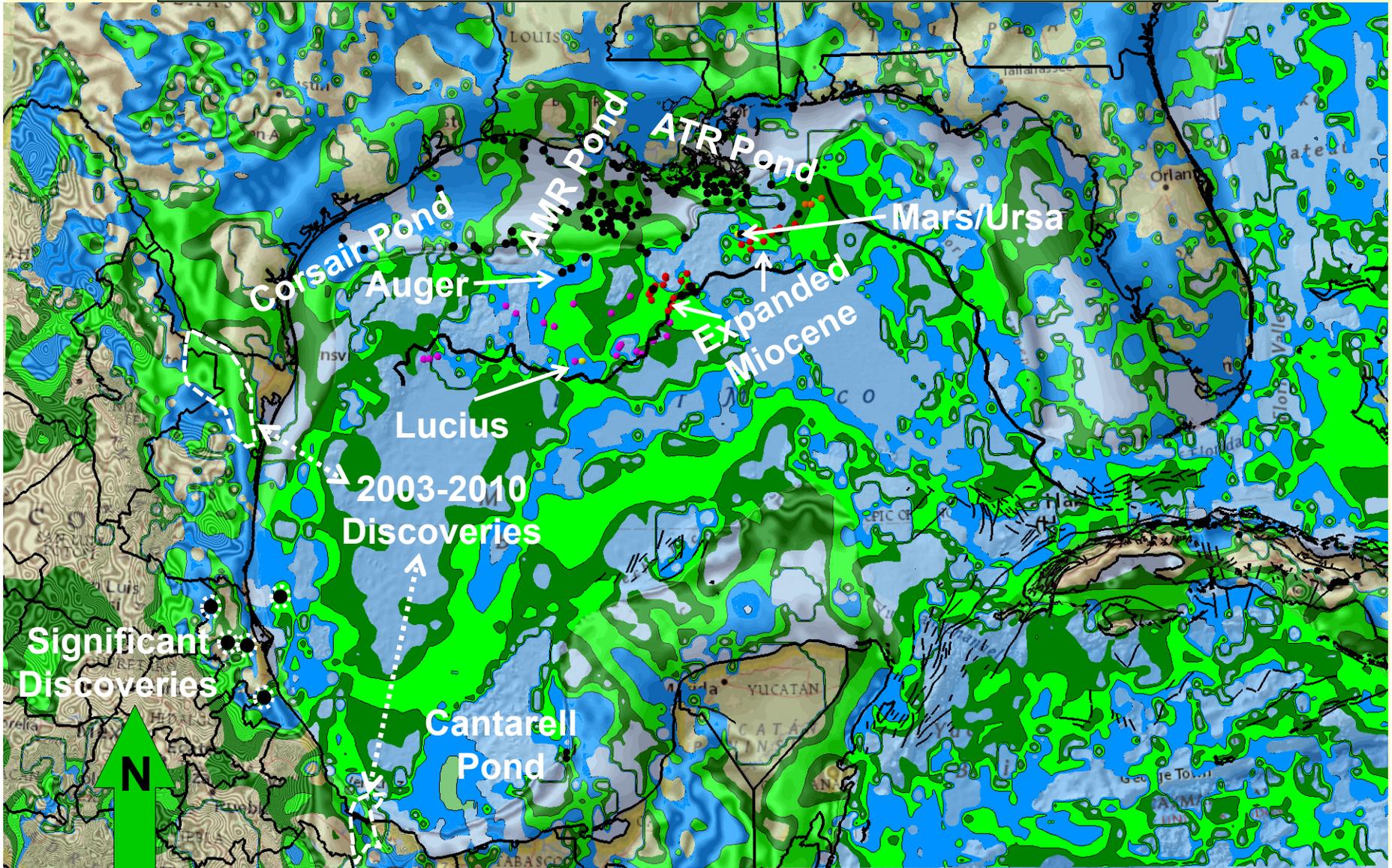
BSMT RIDGES



MOUNDED & PONDED FACIES

R_0 BETWEEN 0 AND -3

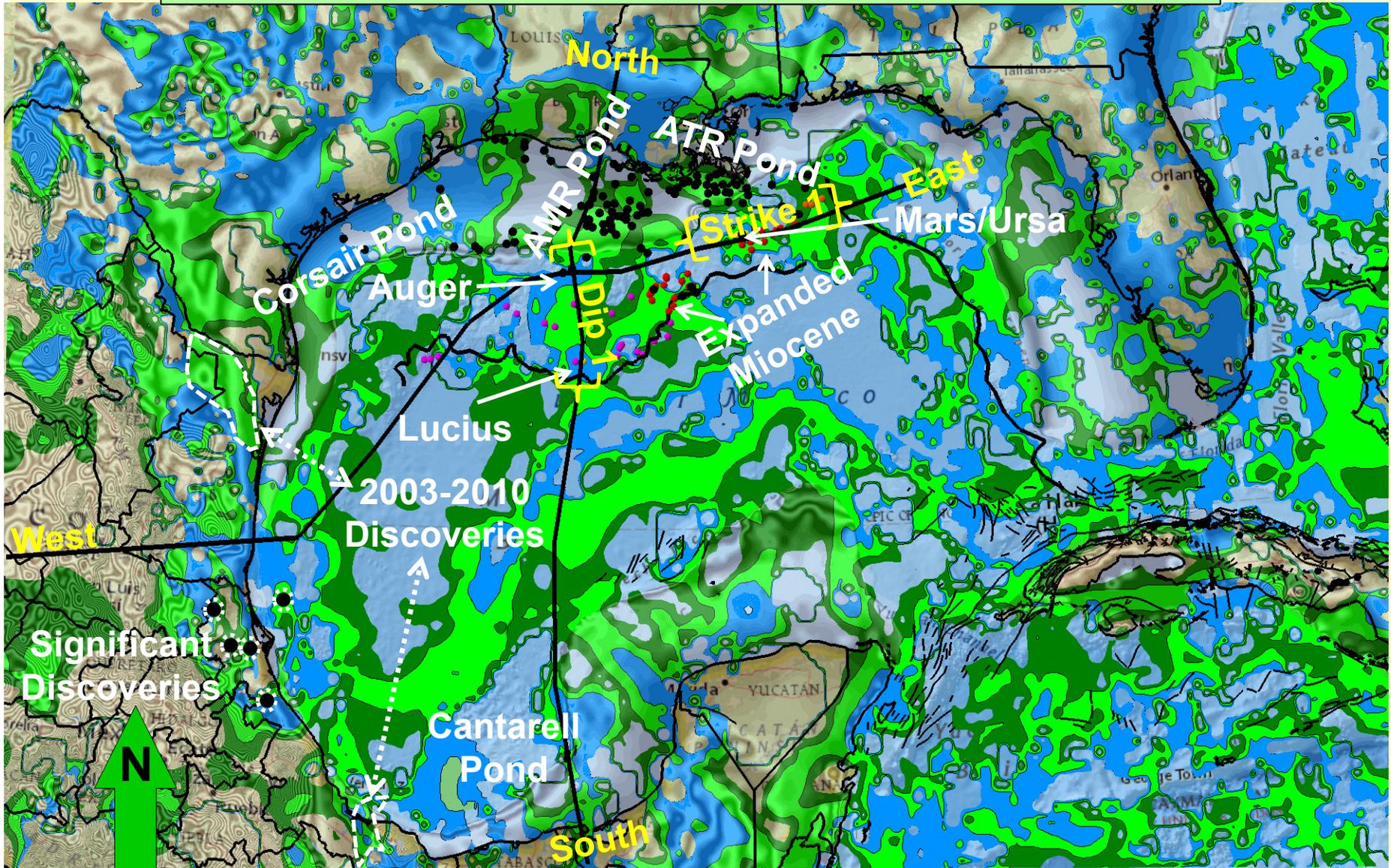
• 103 FIELDS (~77 %) with Current Production > 100 MMBOE



MOUNDED & PONDED FACIES

R₀ BETWEEN 0 AND -3

• **103 FIELDS (~77 %) with Current Production > 100 MMBOE**





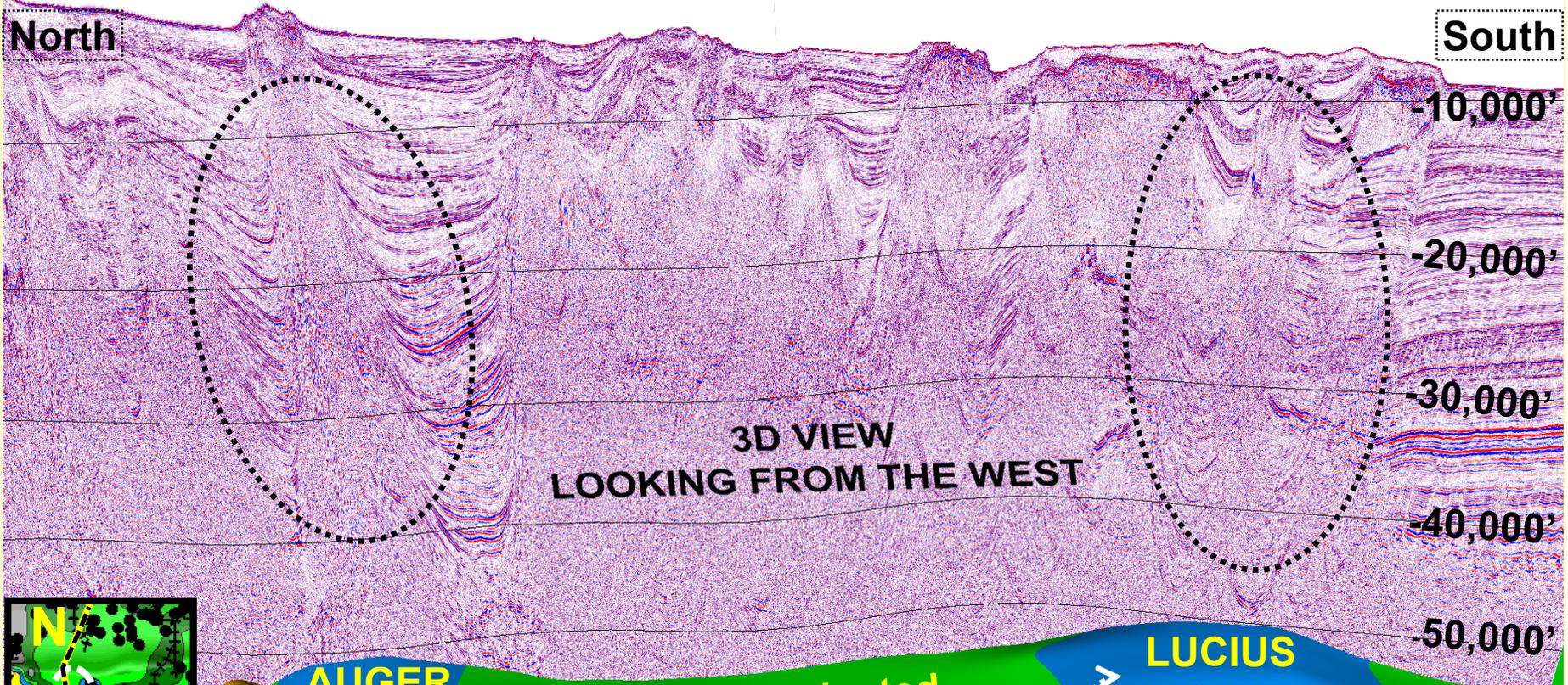
GULFSPAN 2D (PSDM) 2003/04 VINTAGE



DIP 1



Courtesy of ION Geophysical



AUGER MOUND

**Salt-Dominated
Lower Tertiary Pond**

LUCIUS MOUND

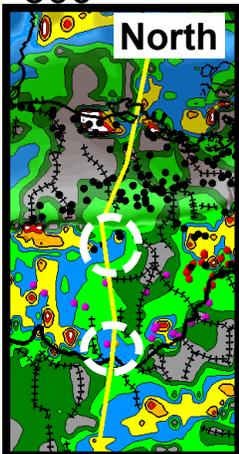
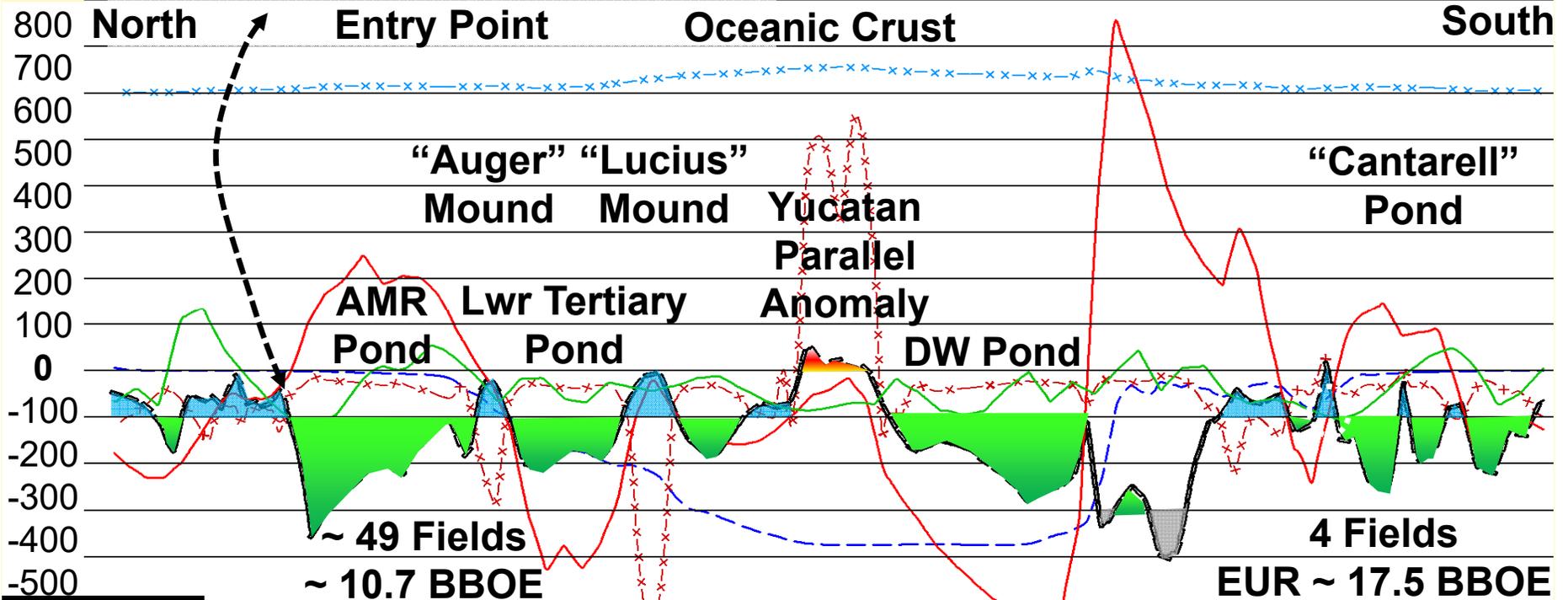
Ro SCALED FOR SEISMIC

Vertical Exaggeration ~ 7.5 to 1



VERTICAL INTERSECTION EXTENDED ALONG & BEYOND DIP1 LINE

Ancestral Mississippi River (AMR)



Gravity Anomaly

Magnetic Anomaly

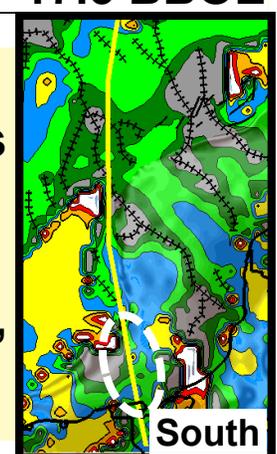
Bathymetry / 10 (Mtr) - - -

FDBG * 1000 x-x-x

FDMG * 100 x-x-x

Ro * 100

DW Pond
Mexican Waters
“Cantarell” Pond





GULFSPAN 2D (PSDM) 2003/04 VINTAGE



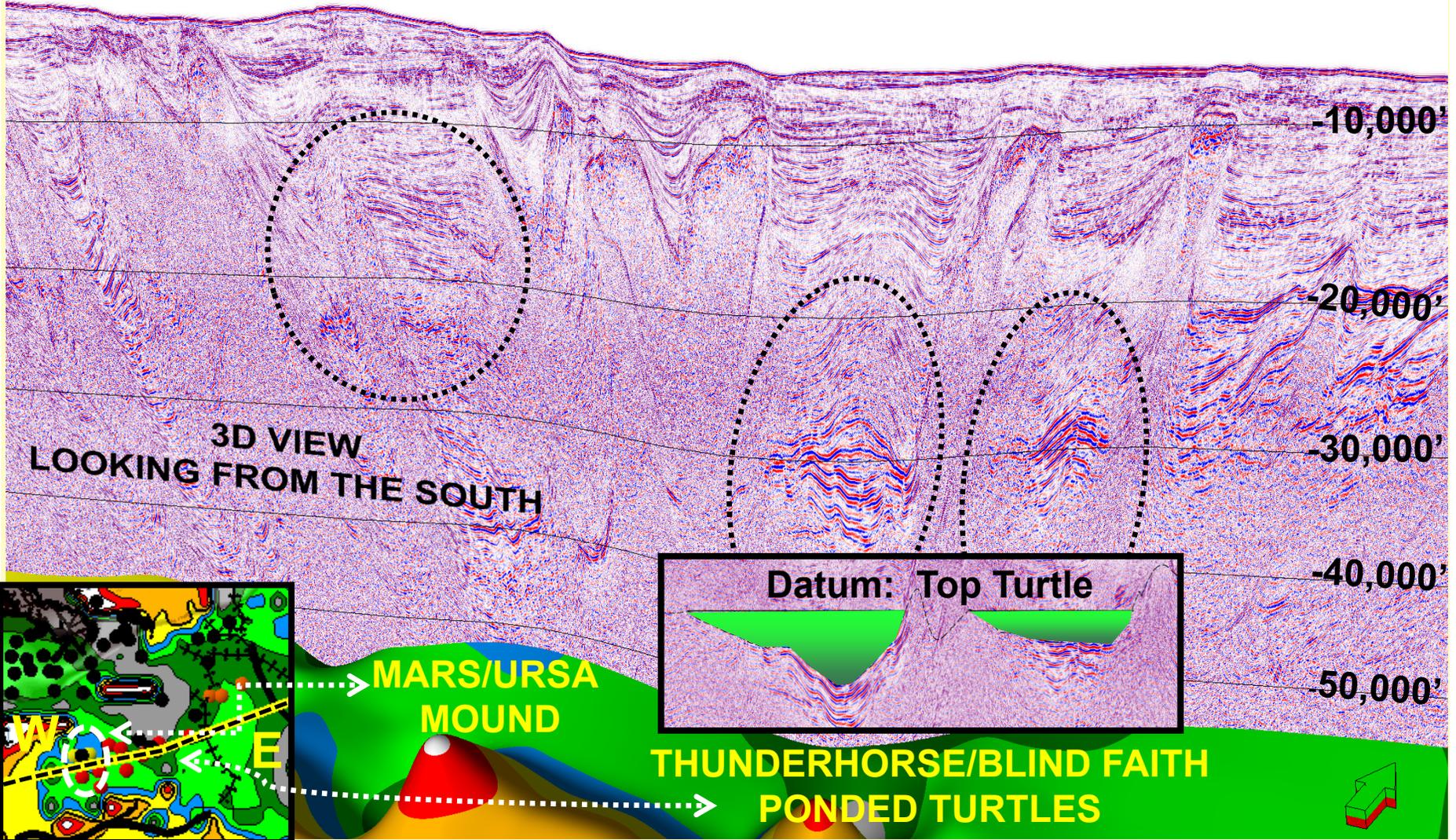
STRIKE 1



Courtesy of ION Geophysical

West

East

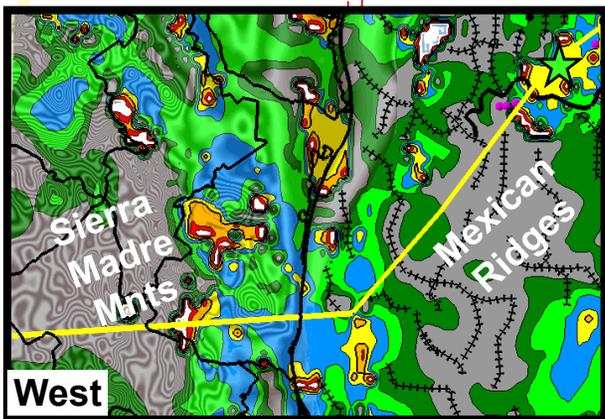
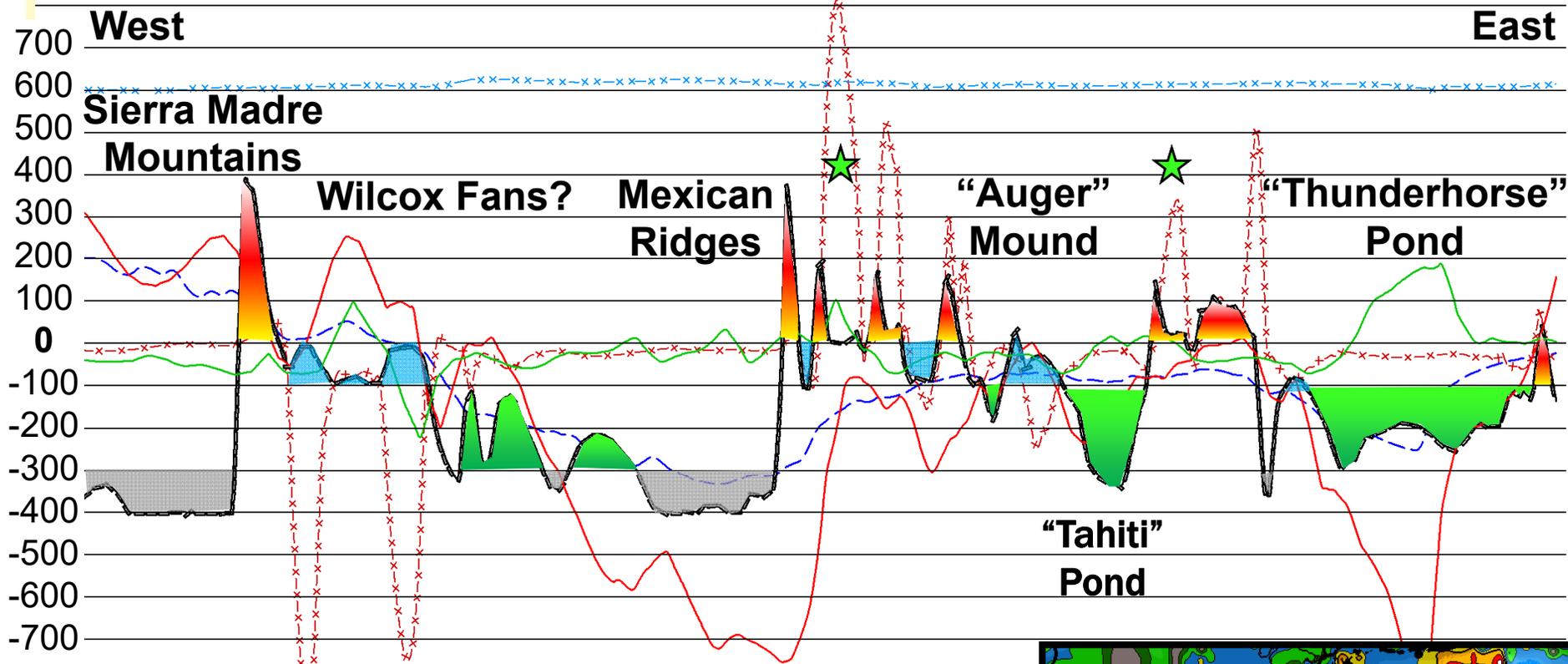


R₀ SCALED FOR SEISMIC

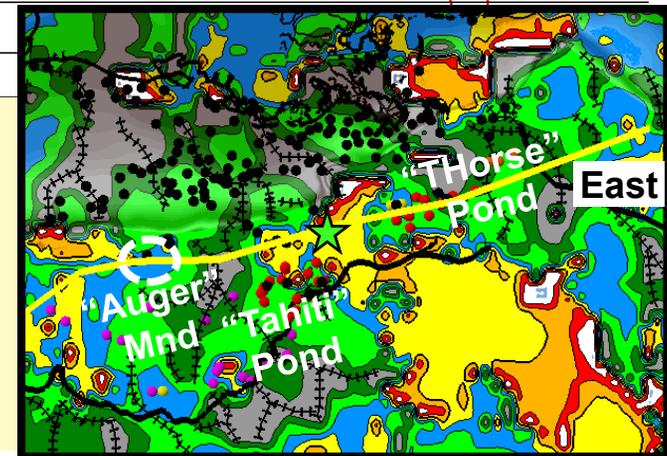
Vertical Exaggeration ~ 7.5 to 1



VERTICAL INTERSECTION EXTENDED ALONG & BEYOND STRIKE1 LINE



Gravity Anomaly
Magnetic Anomaly
Bathymetry / 10 (Mtr) - - -
FDBG * 1000 x-x-x
FDMG * 100 x-x-x
Ro * 100

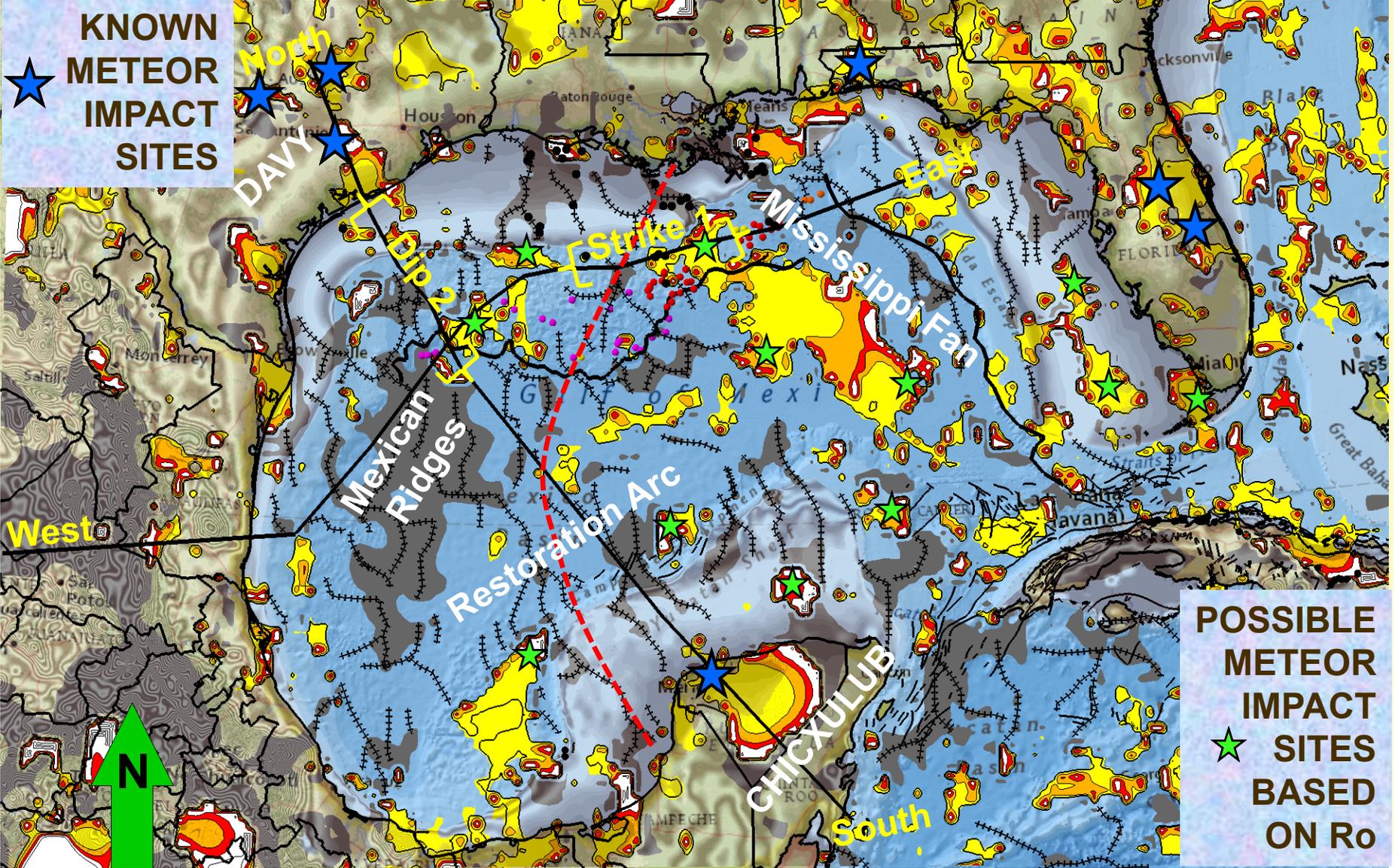


BSMENT HIGHS & PLANAR FACIES

R_o LESS THAN -3 & $R_o > 0$

31 FIELDS with Current Production > 100 MMBOE

BSMT RIDGES



★ KNOWN METEOR IMPACT SITES

★ POSSIBLE METEOR IMPACT SITES BASED ON R_o



GULFSPAN 2D (PSDM) 2003/04 VINTAGE



DIP 2



Courtesy of ION Geophysical

North

South

3D VIEW
LOOKING FROM THE SOUTHWEST

-10,000'

-20,000'

-30,000'

-40,000'

-50,000'



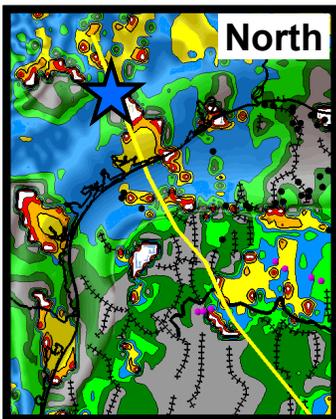
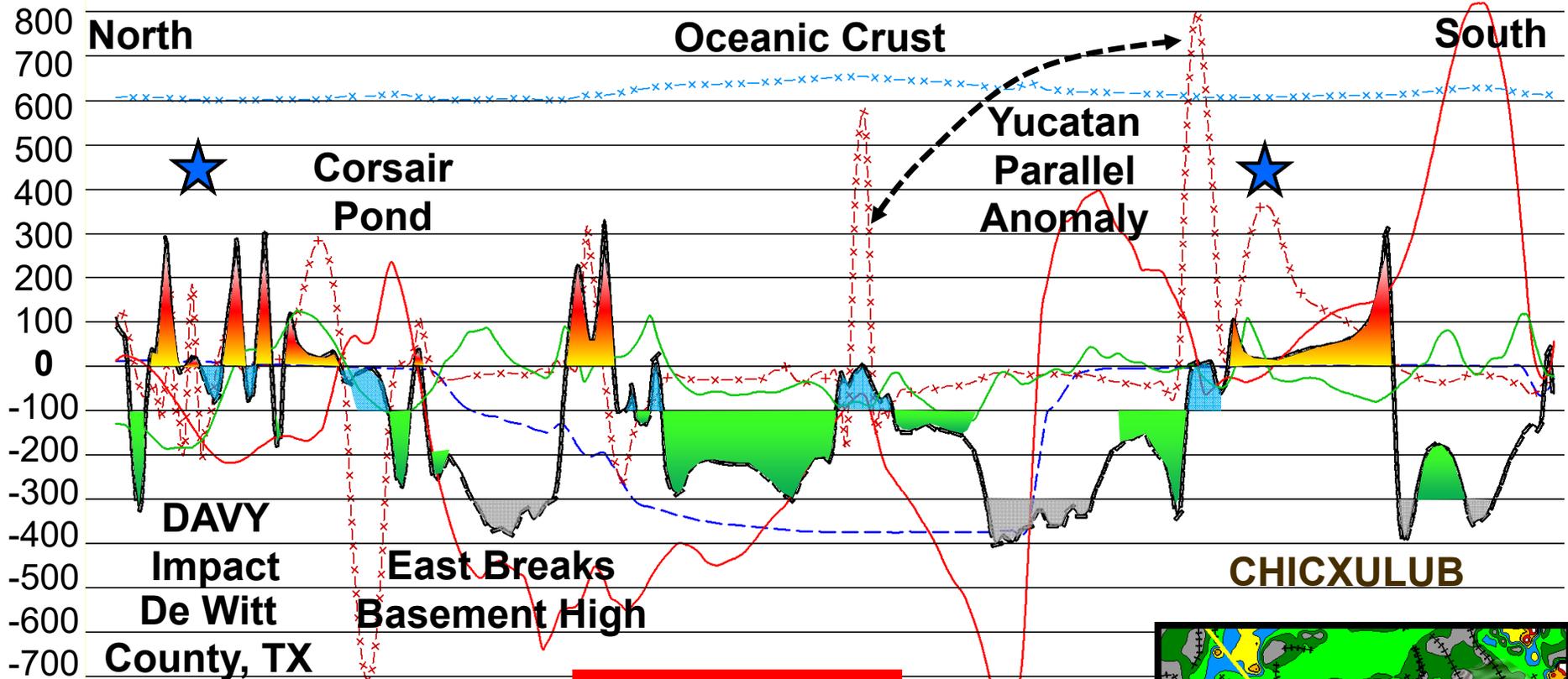
CORSAIR POND
CORSAIR BASEMENT
HIGH

Ro SCALED FOR SEISMIC

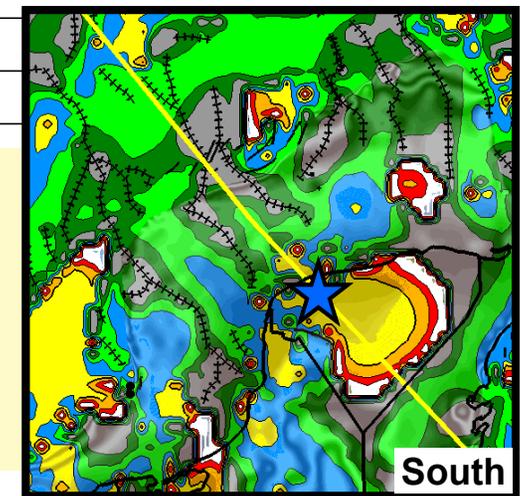
Vertical Exaggeration ~ 7.5 to 1



VERTICAL INTERSECTION EXTENDED ALONG & BEYOND DIP2 LINE



- Gravity Anomaly**
- Magnetic Anomaly**
- Bathymetry / 10 (Mtr) - - -**
- FDBG * 1000 x-x-x**
- FDMG * 100 x-x-x**
- Ro * 100**





GULFSPAN 2D (PSDM) 2003/04 VINTAGE

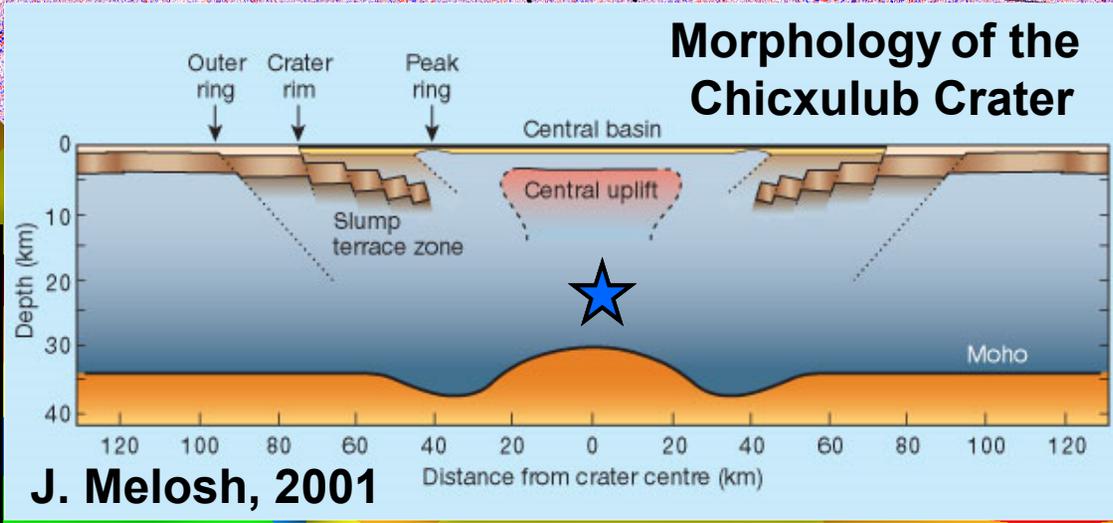
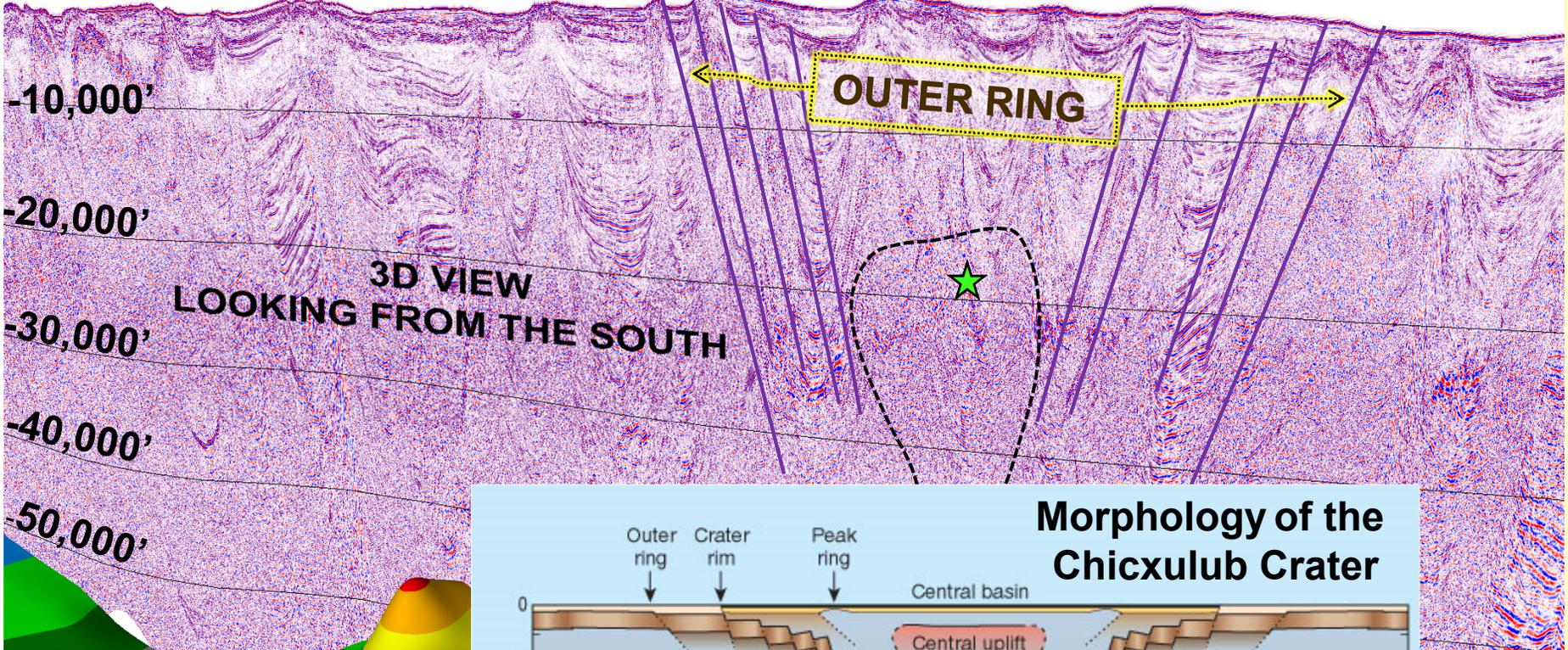
STRIKE 1



ion Courtesy of ION Geophysical

West

East

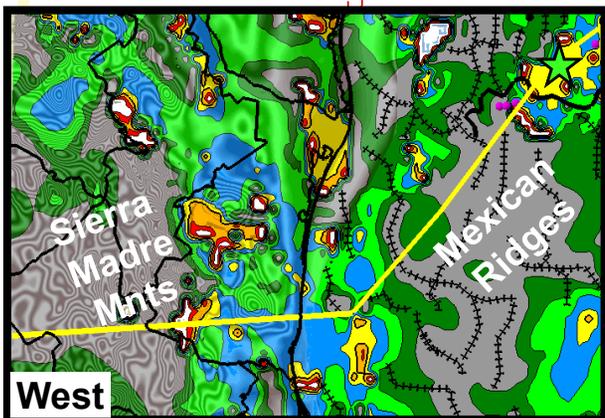
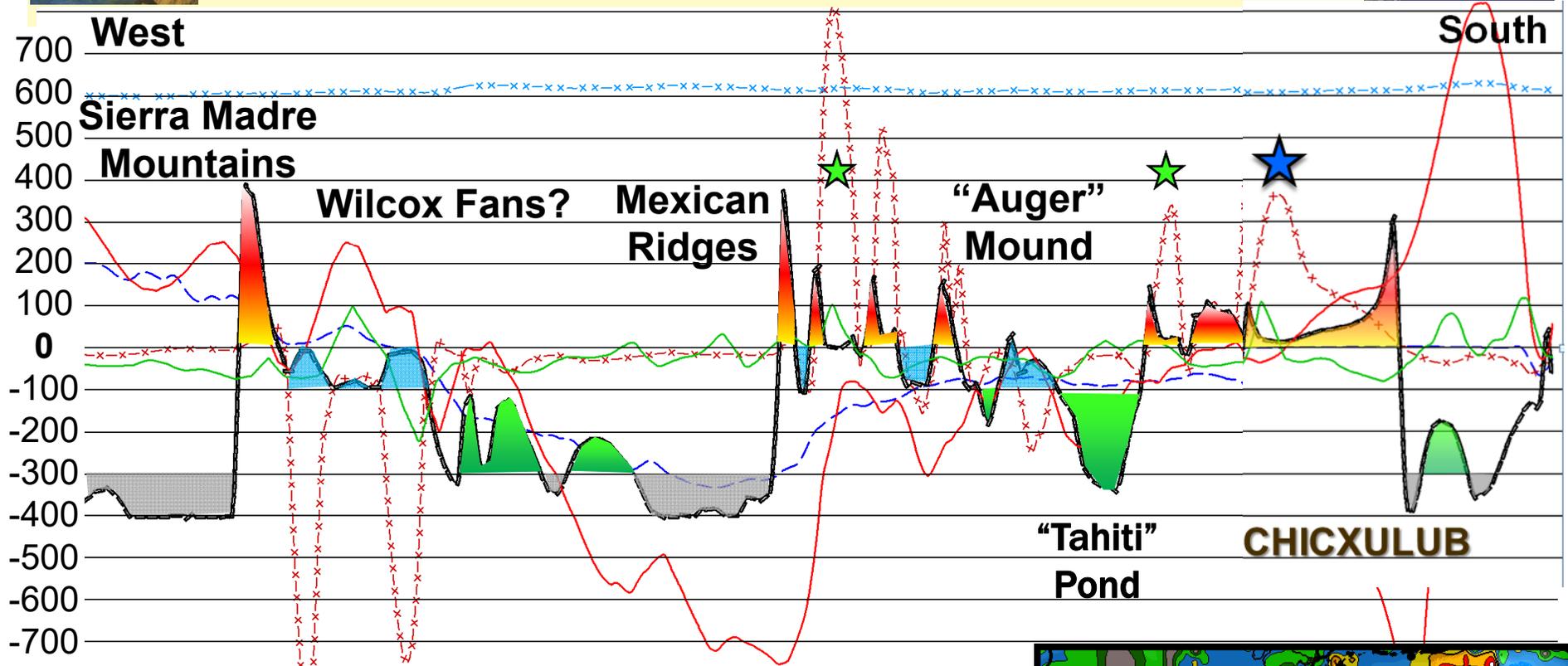


Ro SCALED FOR SEISMIC

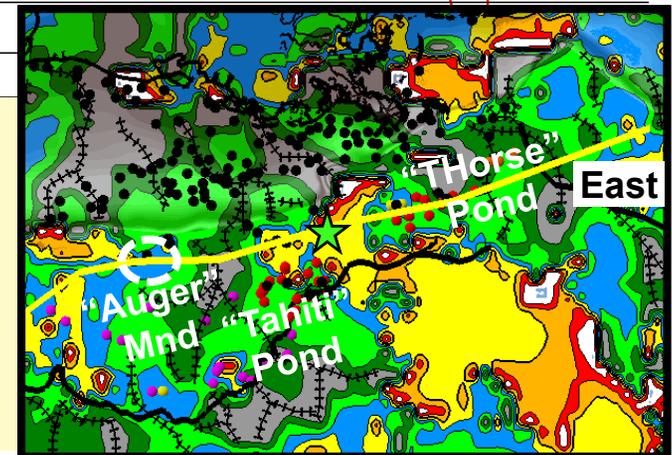
Vertical Exaggeration ~ 7.5 to 1



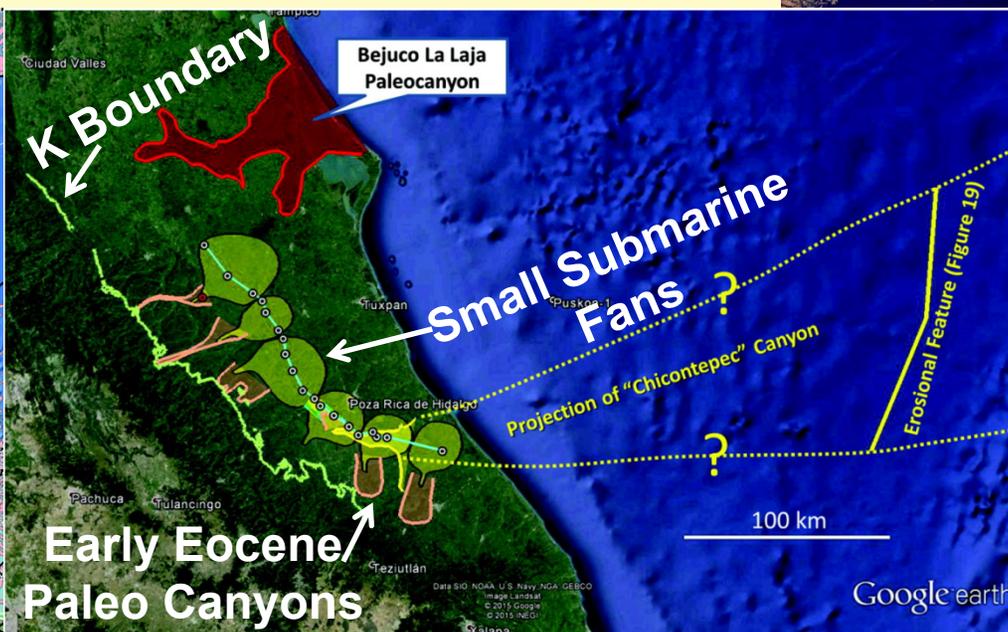
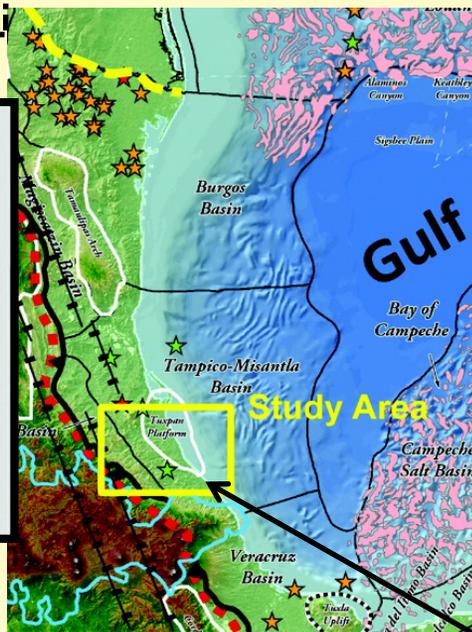
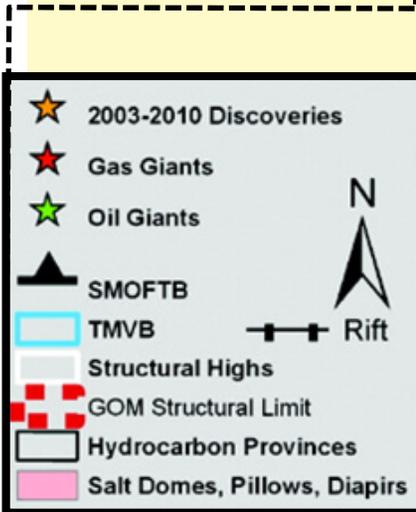
VERTICAL INTERSECTION EXTENDED ALONG & BEYOND STRIKE1 LINE



Gravity Anomaly
Magnetic Anomaly
 Bathymetry / 10 (Mtr) - - -
 FDBG * 1000 x-x-x
 FDMG * 100 x-x-x
 Ro * 100

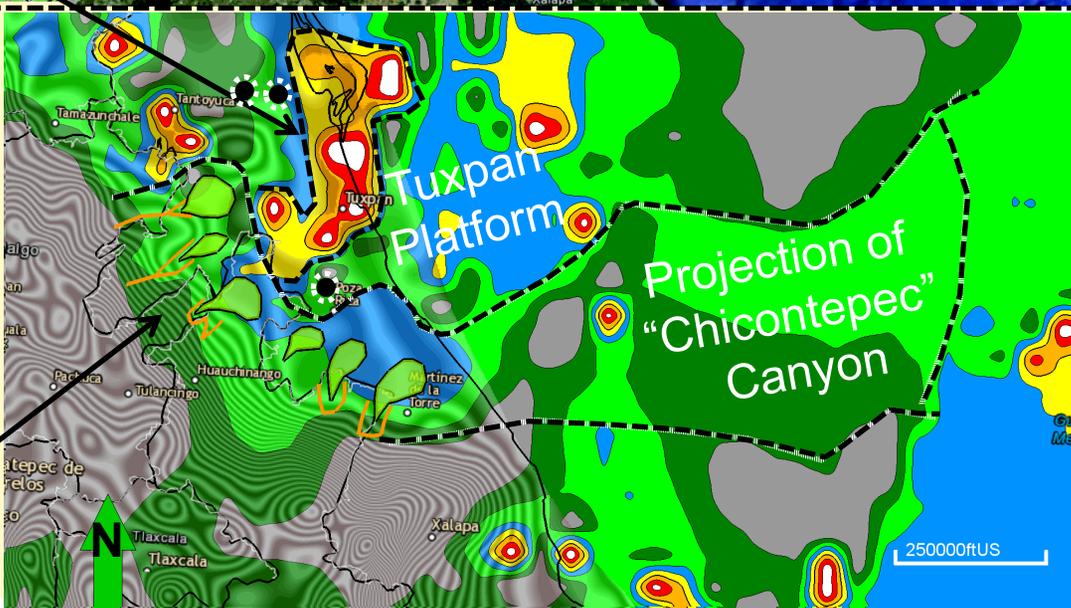


WILCOX PALEOCANYONS IN EASTERN MEXICO SEG INTERPRETATION/FEBRUARY 2016



COMPELLING EVIDENCE FROM EASTERN MEXICO FOR A LATE PALEOCENE /EARLY EOCENE ISOLATION, DRAWDOWN, AND REFILL OF THE GOM. S. COSSEY ET AL.

Area of Wilcox Paleo Canyons and Submarine Fans on Ro





WESTERN MAIN TRANSFORM FAULT (WMTF) SEG INTERPRETATION/FEBRUARY 2016



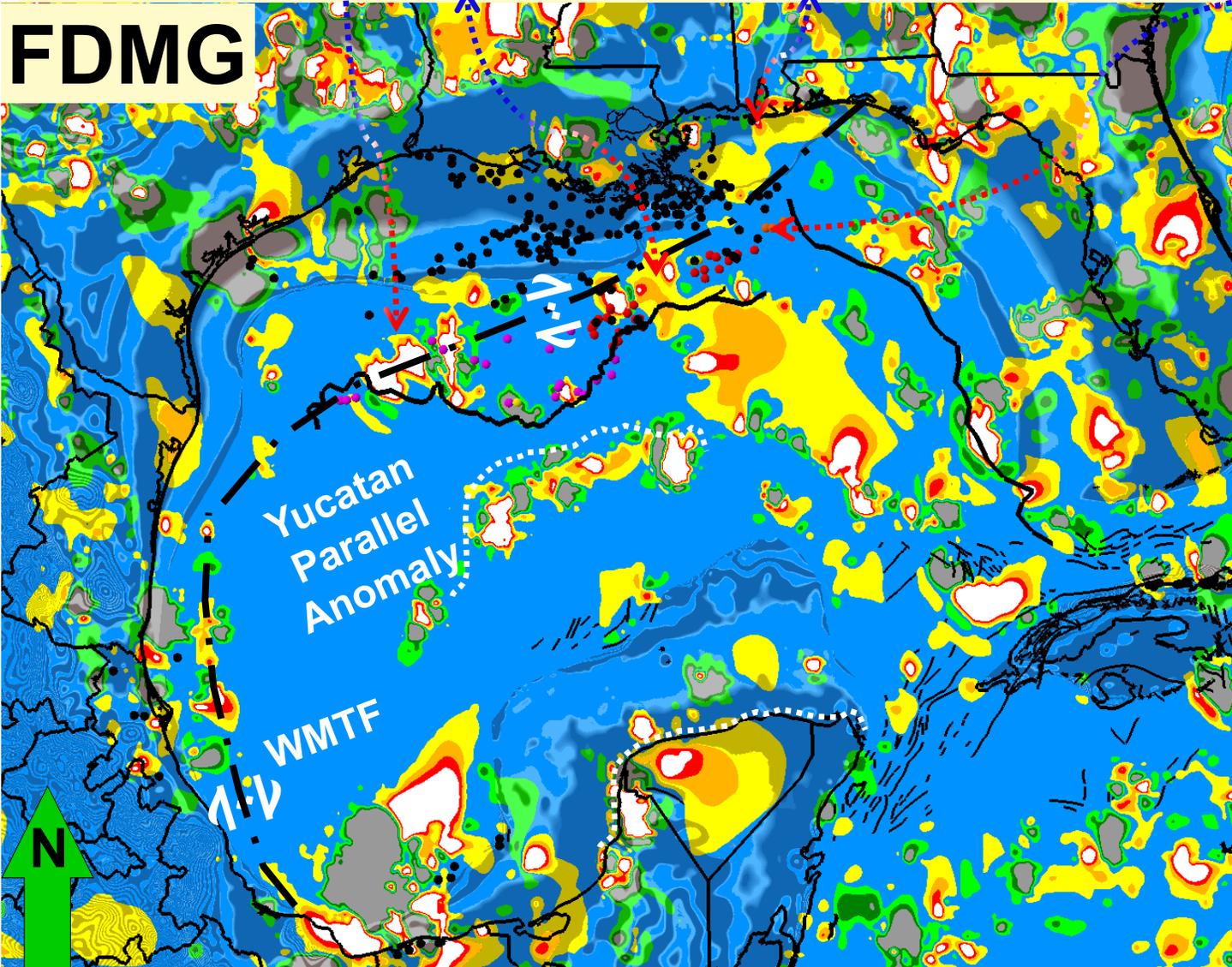
“Norton” Jurassic
@ ~9,000’

“Swan Valley”
Jurassic @ ~12,000’

“Mary Ann Field”
Jurassic @ ~21,000’

“Appomatox Field”
Jurassic @ ~24,000’

FDMG

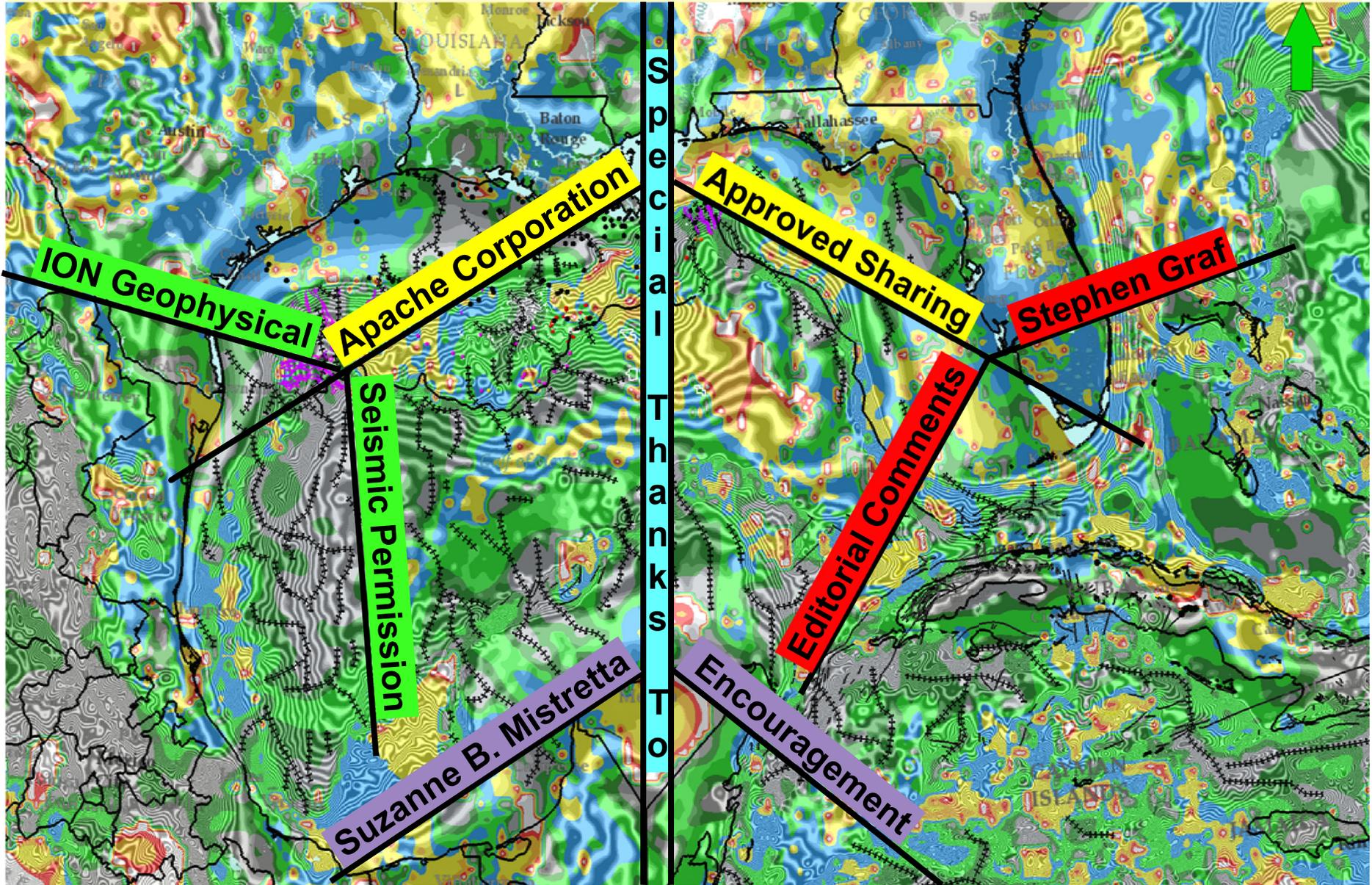


Gravity and Magnetic constraints on the Jurassic opening of the oceanic GoM and the location and tectonic history of the Western Main Transform Fault along the eastern continental margin of Mexico

Nguyen & Mann



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